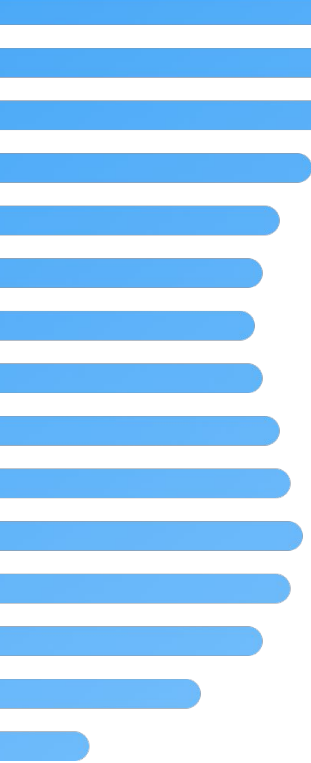
Intro to Time Complexity

Nueva C Compiler | 1 October 2021

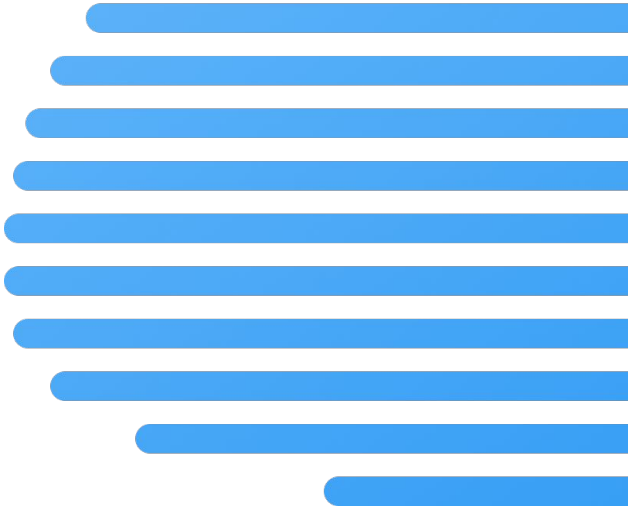


Goal:

evaluate how long things take

Approach:
count the number of operations used

Examples



How many operations?

```
int fn(int n) {
```

```
int x = 1;
x += 1;
```

```
int x = 0;
for (int i=1; i<10; ++i)
{
    x += 1;
}
```

```
return x; }
```

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How many operations?

```
int fn(int n) {
```

A polynomial representation:

A + C*n

```
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{
    x += 1;
}
```
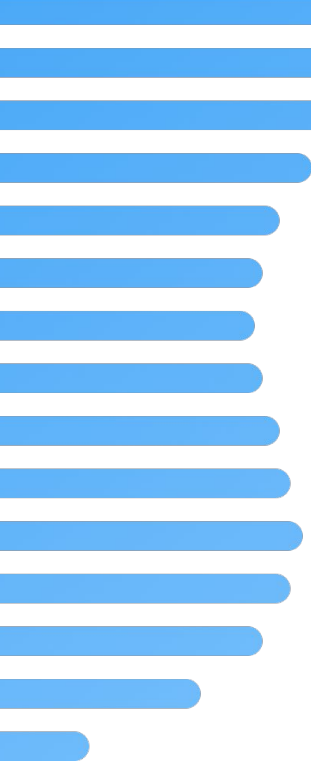

```
return x; }
```



Constant factors are ever changing...

we only care about how the polynomial scales

How many operations?

```
int fn(int n) {
```

```
int x = 1;
x += 1;
```

O(2)

```
int x = 0;
for (int i=1; i<10; ++i)
{
    x += 1;
}
```

O(12)

```
return x; }
```

How many operations?

```
int fn(int n) {
```

```
int x = 1;
x += 1;
```

O(1)

```
int x = 0;
for (int i=1; i<10; ++i)
{
    x += 1;
}
```

O(1)

```
return x; }
```

How many operations?

```
int fn(int n) {
```

A polynomial representation:

A + C*n

```
int x = 0;
for (int i=1; i< n; ++i)
{
    x += 1;
}
```

```
return x; }
```

How many operations?

```
int fn(int n) {
```

A polynomial representation:

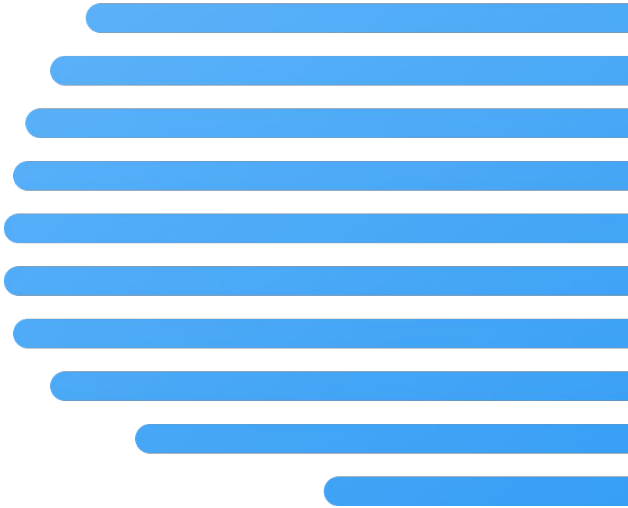
$$\lim_{x \to \infty} \; A + C*n$$

O(n)

```
int x = 0;
for (int i=1; i< n; ++i)
{
    x += 1;
}
```

```
return x; }
```

Practice



What's the time complexity?

```
int fn(int n) {
    int x = 1;
    for (int i=1; i<2*n; ++i)
    {

        x += x;

    }
                                return x; }
```

What's the time complexity?

```
int fn(int n) {
    int x = 1;
    for (int i=1; i<2*n; ++i)
    {
        for (int j=1; j<n; ++j)
        {
            x += x;
        }
    }

    return x; }
```

What's the time complexity?

```
int fn(int *arr, int n) {
    for (int i=1; i<n; ++i)
    {
        for (int j=0; j+i<n; ++j)
        {
            if (arr[j] > arr[j+1])
            {
                swap(arr[j], arr[j+1]);
            }
        }
    }                                   return x; }
```

What's the time complexity?

```
int fn(int base, int exp) {
    int ret = 1;
    while (exp)
    {
        if (exp % 2 == 1)
            ret *= base;
        base *= base;
        exp /= 2;
    }

                                return ret; }
```

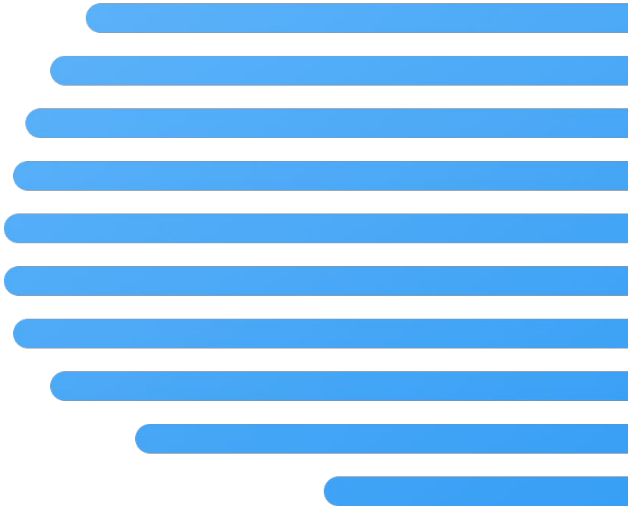
What's the time complexity?

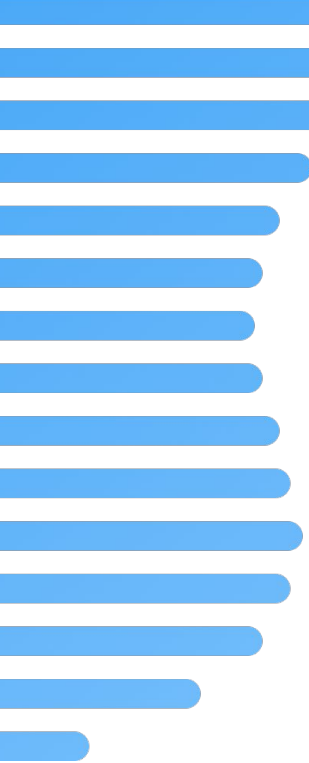
```
int fn(int base, int exp) {
    if (exp <= 0) return 1;

    int ret = fn(base, exp/2);
    ret *= ret;
    if (exp % 2 == 1)
        ret *= base;
    return ret;
}
```

What's the time complexity?

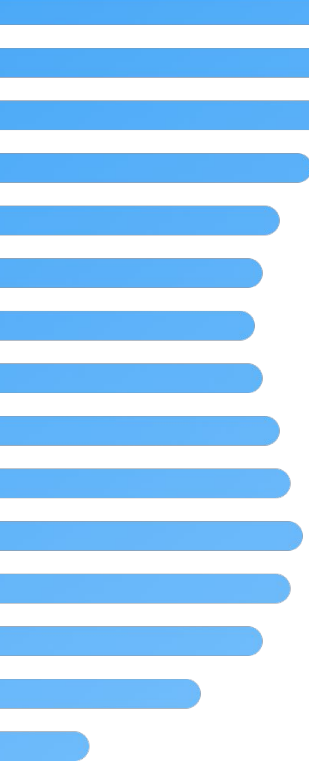
```
int fn(int base, int exp, int v=1) {
    if (exp <= 0) return v;

    if (exp % 2 == 1)
        return fn(base*base, exp/2, v*base);
    else
        return fn(base*base, exp/2, v);
}
```

Problems

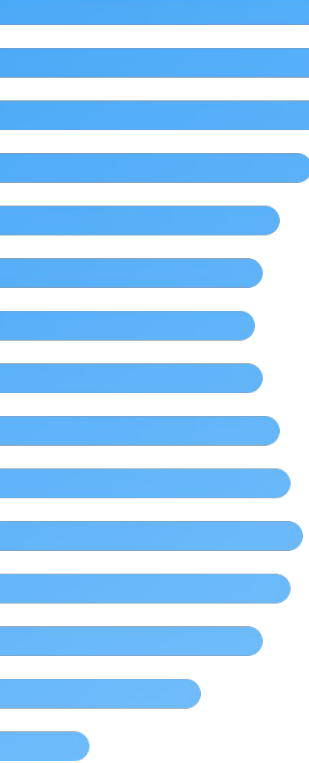




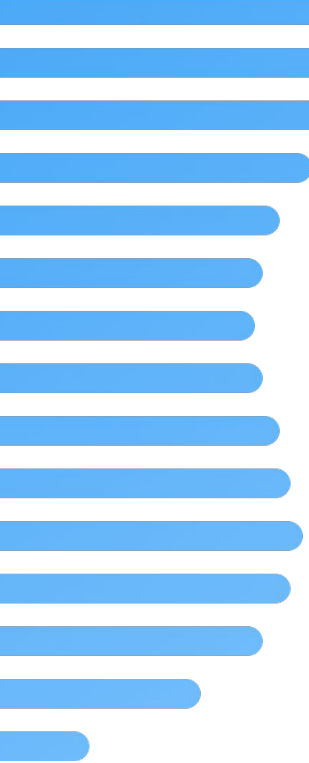
Given a list of N numbers
in the range 0 to 1e9,
see if x is in the list.



Sort a list of N numbers
in the range 0 to 1e9



Sort a list of N numbers
in the range 0 to 1e4



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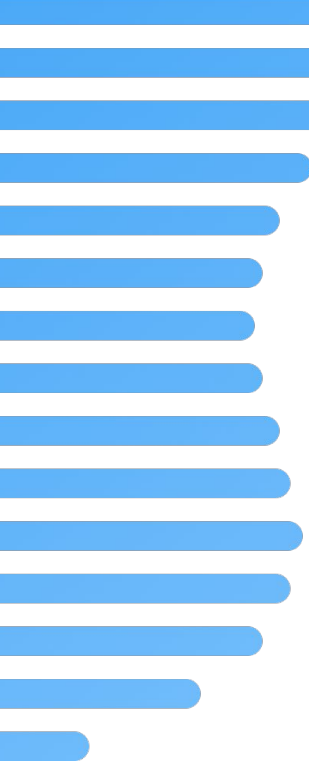
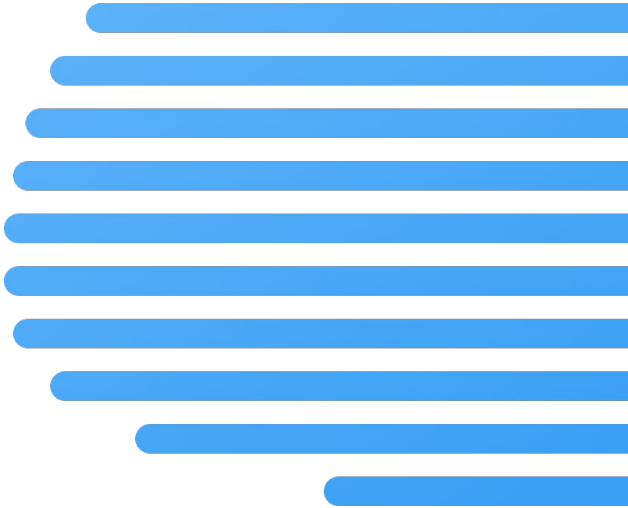


Insert into the front of an array of numbers

Practical Considerations



Arrays vs Lists

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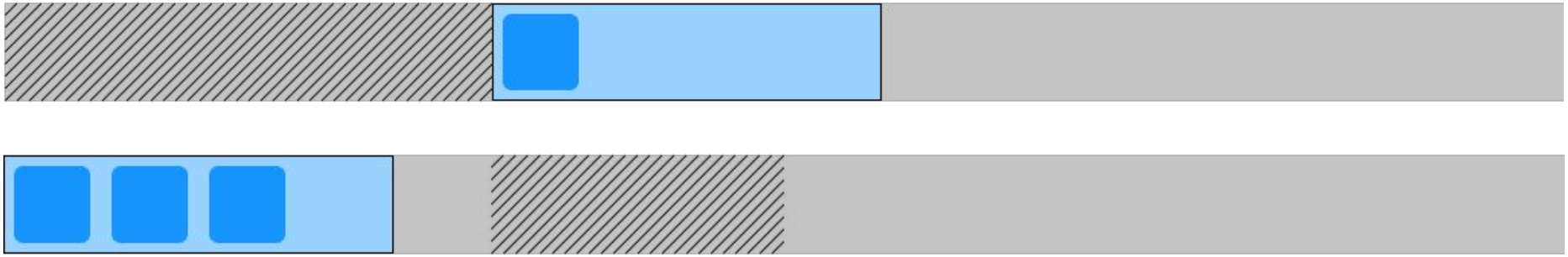
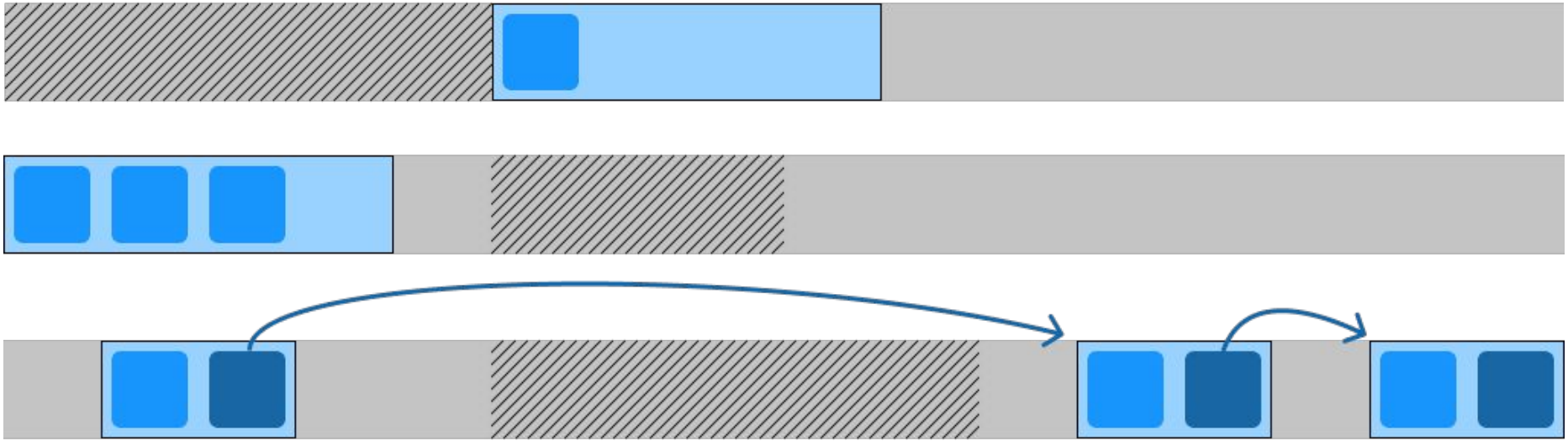
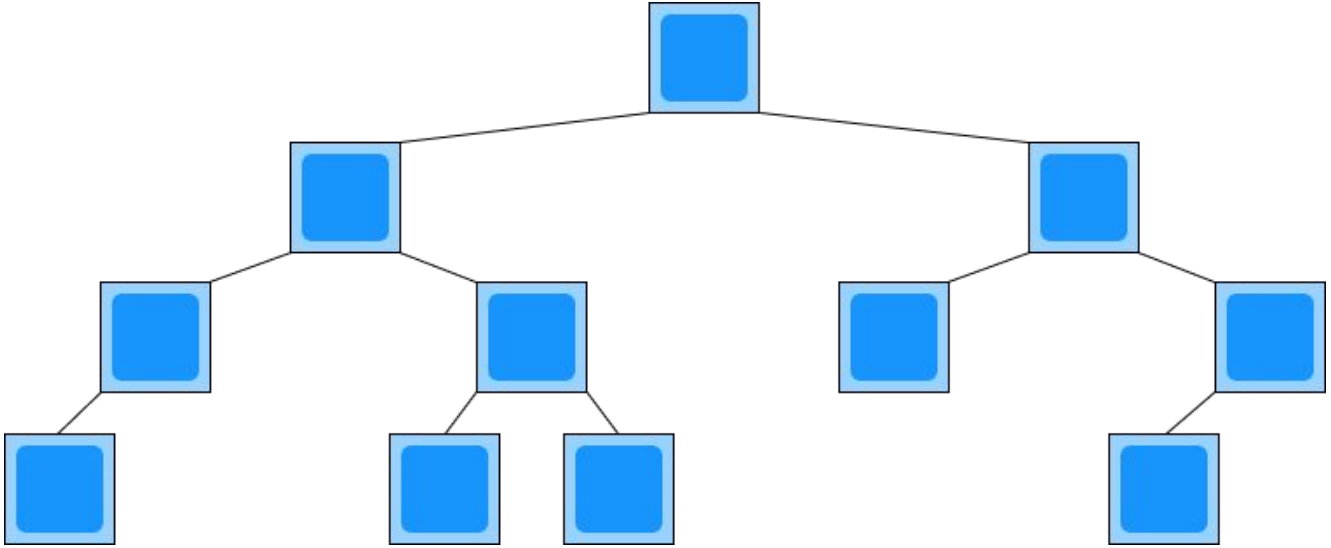


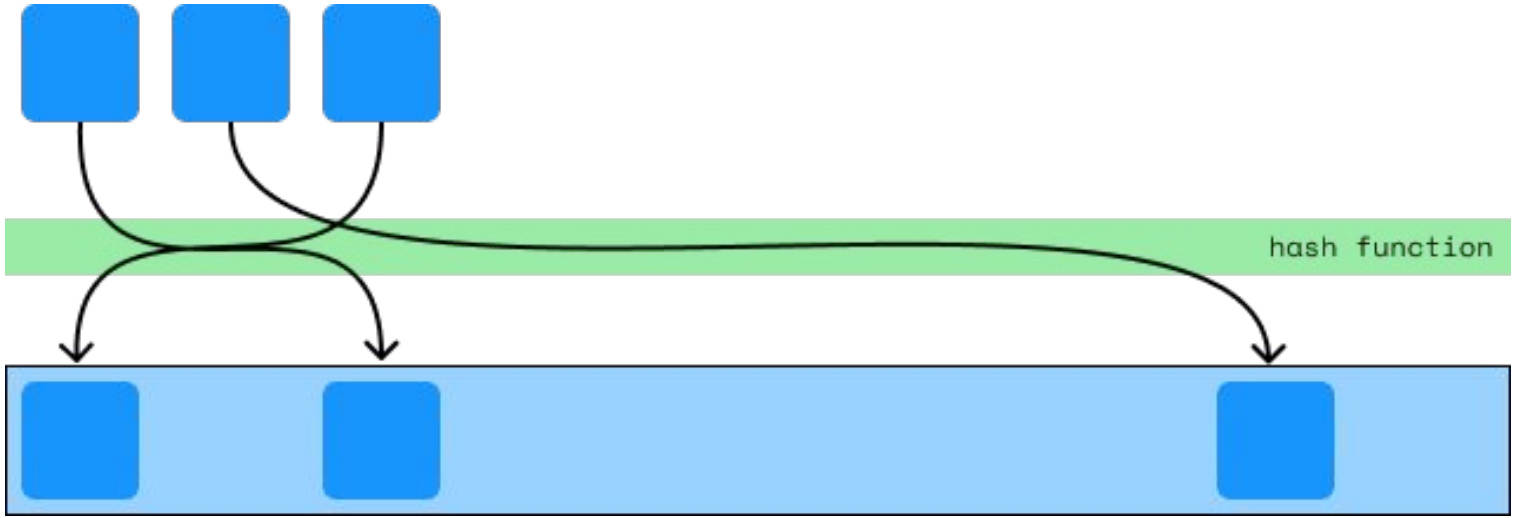
Arrays vs Lists



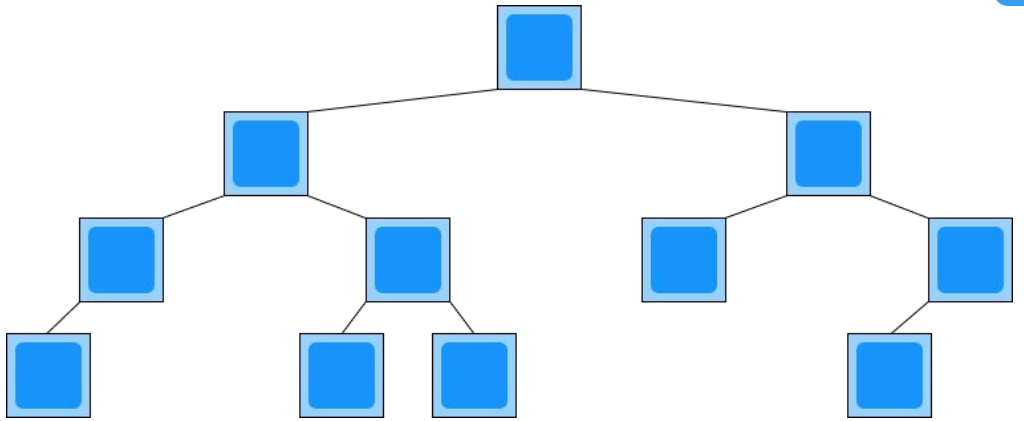
Tree Maps and Hash Maps

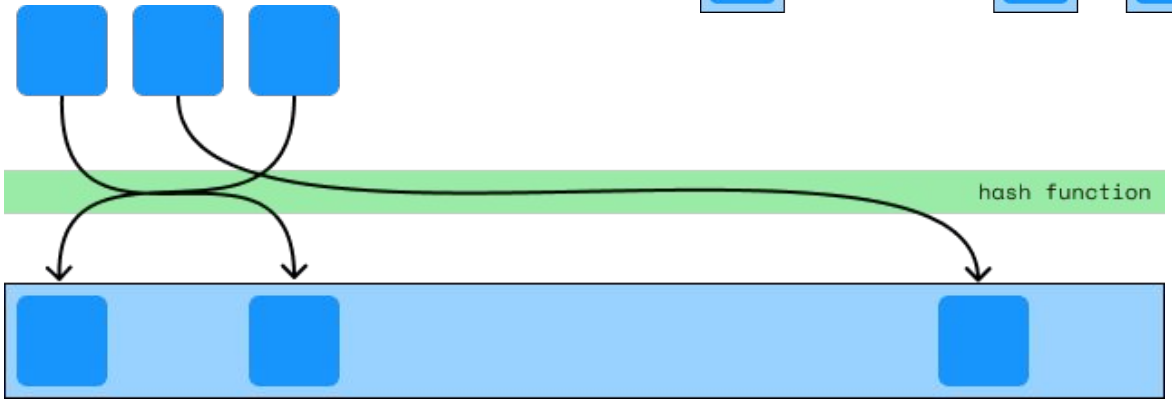


Tree Maps and Hash Maps



Tree Maps and Hash Maps





Constant Factors **Recursive Frames**

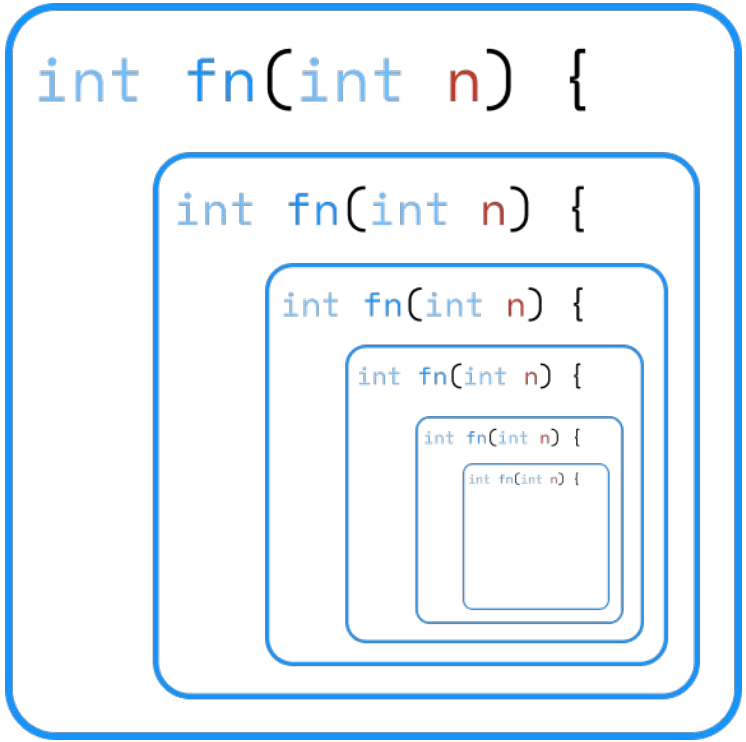
```
int fn(int n) {
```

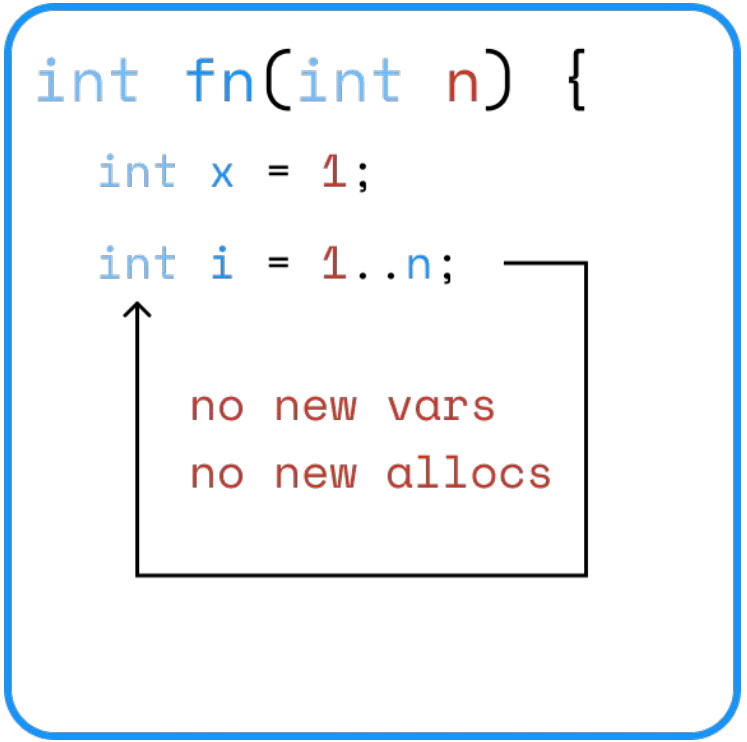
```
if (n == 0) return 1;
int x = fn(n-1) * 2;
```

```
int x = 1;
for (int i=0; i<n; ++i)
{
    x *= 2;
}
```

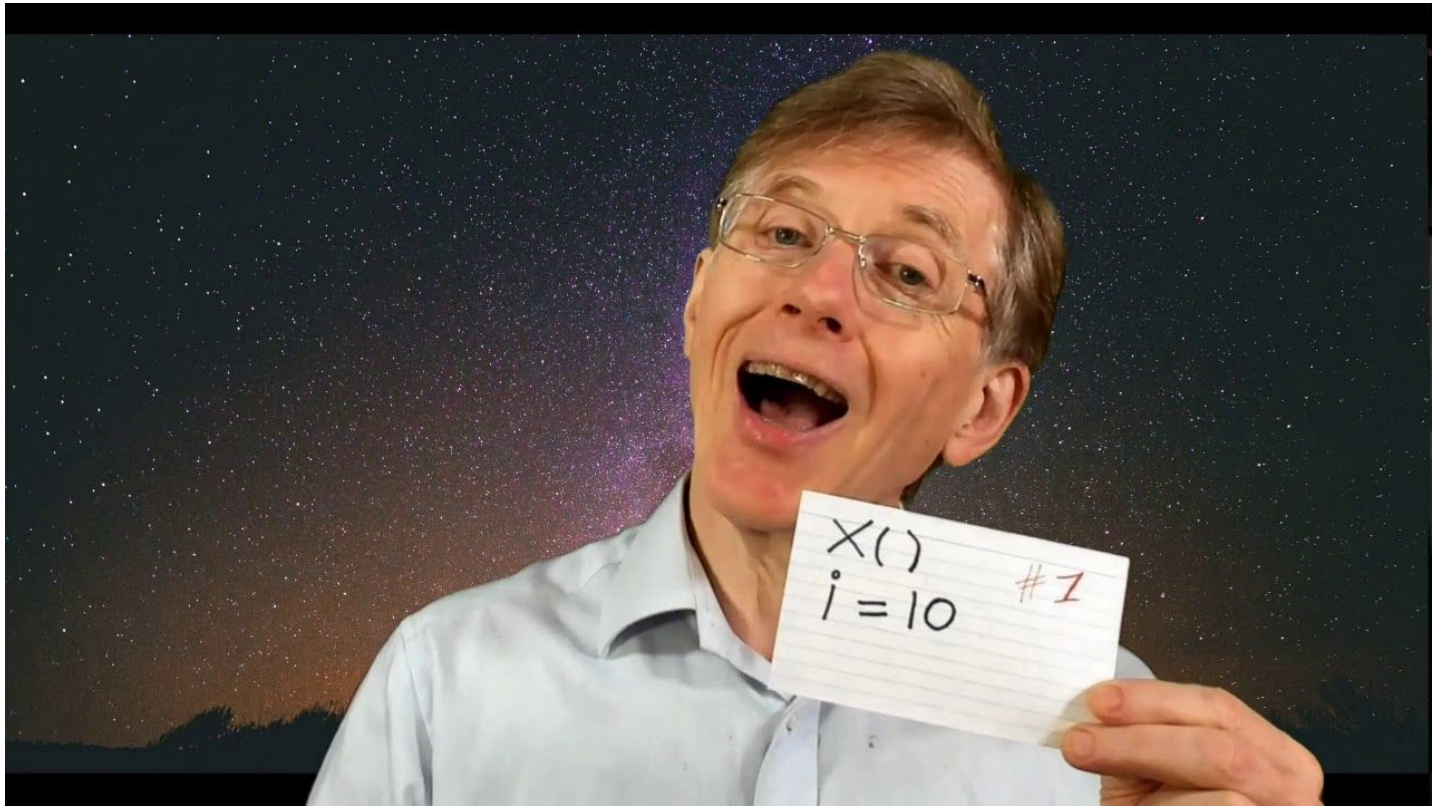
```
return x; }
```

Constant Factors **Recursive Frames**

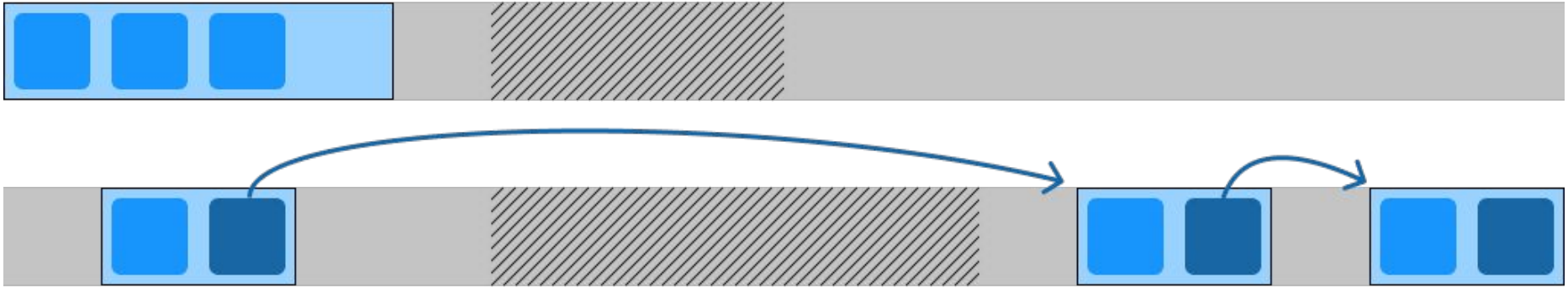




Constant Factors **Recursive Frames**



Constant Factors **Memory Locality**



Constant Factors **Branch Conditions**

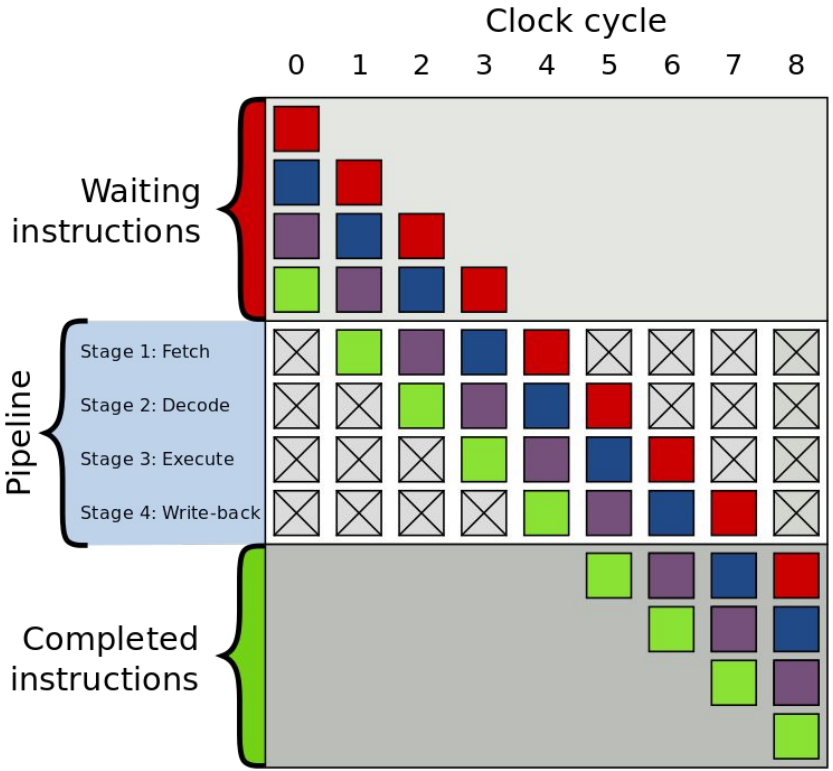
```
int fn(bool x) {
```

```
if (x)
    for (int i=1; i<10; ++i)
    {
        doSomething();
    }
```

```
for (int i=1; i<10; ++i)
{
    if (x)
        doSomething();
}
```

```
}
```

Constant Factors **Branch Conditions**



PROFILE YOUR CODE